CSci 1302 Assignment 9 Due Wedn. Nov. 24th

Algorithm analysis.

Problem 1 (6 points). Prove the following statements:

```
1. n^3 + 1 \in O(n^3 - 1)
2. n^3 - 1 \in O(n^3 + 1)
3. 20n^2 + 100 \in O(n^3 + 1)
```

Problem 2 (6 points) Consider the following algorithm for reversing the order of elements in an array (written in a Java-like syntax):

```
// Given: an array a[n] of n integer elements
// Result: the elements of the array are reversed.
// The index of the first element is 1

int i = 1;
int j = n;
while (i < j) {
    // switching the i-th and the j-th elements
    int temp = a[i];
    a[i] = a[j];
    a[j] = temp;
    i = i + 1;
    j = j - 1;
}</pre>
```

Show how the algorithm works on the array [1, 2, 3, 4]. Compute the runtime of the algorithm based on the number of assignment statements (note that there are 3 assignments in each run of the loop). Give the "Big-O" approximation for the run-time (i.e. O(n), $O(n^2)$, etc.). Show your computations.

Problem 3 (6 points) Consider another algorithm for reversing elements of an array. This algorithm is recursive, so we write it as a recursive function. You may assume that the number of elements in the array is a power of 2. We use the notation a[i..i] to denote a portion of the array from index i to index j.

The idea of the algorithm is to divide the array in half, reverse each sub-array recursively, and then switch the two halves.

```
// Given: an array a[n] of n integer elements
// Result: the elements of the array are reversed.
// The index of the first element is 1
void reverse (a[1..n]) {
```

```
if (n < = 1) return; // do nothing
else {
    reverse (a[1..n/2]);
    reverse (a[((n/2) + 1)..n]);
    // switch the two halves:
    int i = 1;
    while (i <= n/2) {
        int temp = a[i];
        a[i] = a[(n/2) + i];
        a[(n/2) + i] = temp; // corrected 4/2/04
        i = i + 1;
    }
}</pre>
```

Show how the algorithm works on the array [1, 2, 3, 4]. What is the running time of the algorithm? What is the "Big-O" approximation for the run-time? Show your computations.

Problem 4 (2 points) Which of the algorithms in the previous two problems would you recommend for reversing an array? Explain your reasoning.